# GCE Examinations Advanced Subsidiary

# **Core Mathematics C4**

Paper A Time: 1 hour 30 minutes

## Instructions and Information

Candidates may use any calculator EXCEPT those with the facility for symbolic algebra, differentiation and/or integration.

Full marks may be obtained for answers to ALL questions.

Mathematical formulae and statistical tables are available.

This paper has seven questions.

### Advice to Candidates

You must show sufficient working to make your methods clear to an examiner. Answers without working may gain no credit.



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#### **1.** A curve has the equation

$$x^2(2+y) - y^2 = 0.$$

(6)

Find an expression for  $\frac{dy}{dx}$  in terms of x and y.

2. 
$$f(x) = \frac{3}{\sqrt{1-x}}, |x| < 1.$$

(a) Show that 
$$f(\frac{1}{10}) = \sqrt{10}$$
. (2)

- (b) Expand f(x) in ascending powers of x up to and including the term in  $x^3$ , simplifying each coefficient. (3)
- (c) Use your expansion to find an approximate value for  $\sqrt{10}$ , giving your answer to 8 significant figures. (1)
- (d) Find, to 1 significant figure, the percentage error in your answer to part (c). (2)
- 3. Relative to a fixed origin, O, the line l has the equation

$$\mathbf{r} = (\mathbf{i} + p\mathbf{j} - 5\mathbf{k}) + \lambda(3\mathbf{i} - \mathbf{j} + q\mathbf{k}),$$

where p and q are constants and  $\lambda$  is a scalar parameter.

Given that the point A with coordinates (-5, 9, -9) lies on l,

(a) find the values of $p$ and $q$ ,	(3)
(b) show that the point B with coordinates $(25, -1, 11)$ also lies on l.	(2)
The point C lies on $l$ and is such that OC is perpendicular to $l$ .	
(c) Find the coordinates of C.	(4)
(d) Find the ratio $AC: CB$	(2)

4. During a chemical reaction, a compound is being made from two other substances. At time t hours after the start of the reaction, x g of the compound has been produced. Assuming that x = 0 initially, and that

$$\frac{\mathrm{d}x}{\mathrm{d}t} = 2(x-6)(x-3),$$

- (a) show that it takes approximately 7 minutes to produce 2 g of the compound. (10)
- (b) Explain why it is not possible to produce 3 g of the compound.

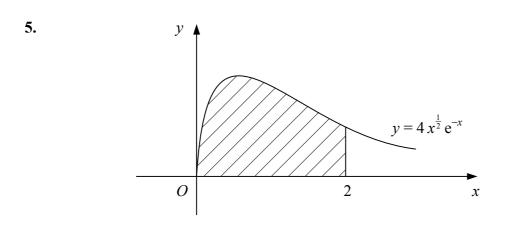




Figure 1 shows the curve with equation  $y = 4 x^{\frac{1}{2}} e^{-x}$ .

The shaded region is bounded by the curve, the *x*-axis and the line x = 2.

(a) Use the trapezium rule with four intervals of equal width to estimate the area of the shaded region. (5)

The shaded region is rotated through  $2\pi$  radians about the *x*-axis.

(b) Find, in terms of  $\pi$  and e, the exact volume of the solid formed. (7)

6. (a) Find

$$2 \sin 3x \sin 2x \, dx.$$
 (4)

(b) Use the substitution  $u^2 = x + 1$  to evaluate

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$$\int_{0}^{3} \frac{x^{2}}{\sqrt{x+1}} \, \mathrm{d}x. \tag{8}$$

Turn over

(2)

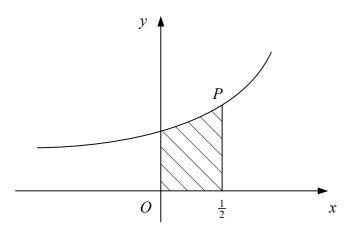


Figure 2

Figure 2 shows the curve with parametric equations

 $x = \cos 2t$ ,  $y = \operatorname{cosec} t$ ,  $0 < t < \frac{\pi}{2}$ .

The point *P* on the curve has *x*-coordinate  $\frac{1}{2}$ .

(a) Find the value of the parameter t at P. (2)

(b) Show that the tangent to the curve at P has the equation

$$y = 2x + 1. \tag{5}$$

(4)

The shaded region is bounded by the curve, the coordinate axes and the line  $x = \frac{1}{2}$ .

(c) Show that the area of the shaded region is given by

$$\int_{\frac{\pi}{6}}^{\frac{\pi}{4}} k \cos t \, \mathrm{d}t,$$

where *k* is a positive integer to be found.

(d) Hence find the exact area of the shaded region. (3)

#### END