

Mark Scheme (Results)

January 2012

GCE Further Pure FP1 (6667) Paper 01

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- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

EDEXCEL GCE MATHEMATICS

General Instructions for Marking

- 1. The total number of marks for the paper is 75.
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- **M** marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- **B** marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.
- 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes and can be used if you are using the annotation facility on ePEN.

- bod benefit of doubt
- ft follow through
- the symbol \bigwedge will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- dep dependent
- indep independent
- dp decimal places
- sf significant figures
- ***** The answer is printed on the paper
- The second mark is dependent on gaining the first mark
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

General Principals for Core Mathematics Marking

(But note that specific mark schemes may sometimes override these general principles).

Method mark for solving 3 term quadratic:

1. <u>Factorisation</u> $(x^{2} + bx + c) = (x + p)(x + q), \text{ where } |pq| = |c| \text{ , leading to } x = \dots$ $(ax^{2} + bx + c) = (mx + p)(nx + q), \text{ where } |pq| = |c| \text{ and } |mn| = |a| \text{ , leading to } x = \dots$

2. <u>Formula</u>

Attempt to use <u>correct</u> formula (with values for a, b and c), leading to x = ...

3. Completing the square

Solving $x^2 + bx + c = 0$: $(x \pm \frac{b}{2})^2 \pm q \pm c, q \neq 0$, leading to x = ...

Method marks for differentiation and integration:

1. Differentiation

Power of at least one term decreased by 1. ($x^{n} \rightarrow x^{n-1}$)

2. Integration

Power of at least one term increased by 1. ($x^n \rightarrow x^{n+1}$)

Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.

Normal marking procedure is as follows:

<u>Method mark</u> for quoting a correct formula and attempting to use it, even if there are mistakes in the substitution of values.

Where the formula is <u>not</u> quoted, the method mark can be gained by implication from <u>correct</u> working with values, but may be lost if there is any mistake in the working.

January 2012 6667 Further Pure Mathematics FP1 Mark Scheme

| Question Number | Scheme | Notes | Marks |
|--------------------|---|--|---------|
| 1(a) | $\arg z_1 = -\arctan(1)$ | $-\arctan(1)$ or $\arctan(1)$ or $\arctan(-1)$ | M1 |
| | $=-\frac{\pi}{4}$ | or -45 or awrt -0.785 (oe e.g $\frac{7\pi}{4}$) | A1 |
| | Correct a | nswer only 2/2 | (2) |
| (b) | $z_1 z_2 = (1 - i)(3 + 4i) = 3 - 3i + 4i - 4i^2$ | At least 3 correct terms (Unsimplified) | M1 |
| | = 7 + i | cao | A1 |
| | | | (2) |
| (c) | $\frac{z_2}{z_1} = \frac{(3+4i)}{(1-i)} = \frac{(3+4i).(1+i)}{(1-i).(1+i)}$ | Multiply top and bottom by $(1 + i)$ | M1 |
| | $=\frac{(3+4i).(1+i)}{2}$ $=-\frac{1}{2}+\frac{7}{2}i$ | (1+i)(1-i) = 2 | A1 |
| | $=-\frac{1}{2}+\frac{7}{2}i$ | or $\frac{-1+7i}{2}$ | A1 |
| | Special case $\frac{z_1}{z_2} = \frac{(1-i)}{(3+4i)} = \frac{(1-i).(3-4i)}{(3+4i).(3-4i)}$ Allow M1A0A0 | | |
| | | | (3) |
| | Correct answers only in | n (b) and (c) scores no marks | Total 7 |

| Question Number | Scheme | Notes | Marks |
|--------------------|--|--|------------|
| 2 | $f(x) = x^4 + x - 1$ | | |
| (a) | $f(0.5) = -0.4375 (-\frac{7}{16})$ $f(1) = 1$ | Either any one of $f(0.5) = awrt - 0.4$ or $f(1) = 1$ | M1 |
| | Sign change (positive, negative) (and $f(x)$ is continuous) therefore (a root) α is between x = 0.5 and $x = 1.0$ | f(0.5) = awrt -0.4 and $f(1) = 1$, sign change and conclusion | A1 |
| | | | (2) |
| (b) | $f(0.75) = 0.06640625(\frac{17}{256})$ | Attempt f(0.75) | M 1 |
| | $f(0.625) = -0.222412109375(-\frac{911}{4096})$ | $f(0.75) = awrt \ 0.07$ and $f(0.625) = awrt \ -0.2$ | A1 |
| | | 0.625 ,, α ,, 0.75 or 0.625 < α < 0.75 | |
| | 0.625 " α " 0.75 | or [0.625, 0.75] or (0.625, 0.75). | A1 |
| | | or equivalent in words. | |
| | In (b) there is no credit for linear interpolation and a | | |
| (c) | correct answer with no working scores no marks. $f'(x) = 4x^3 + 1$ Correct derivative (May be implied later | | |
| (0) | $f'(x) = 4x^3 + 1$ | by e.g. $4(0.75)^3 + 1)$ | B1 |
| | $x_1 = 0.75$ | | |
| | $x_2 = 0.75 - \frac{f(0.75)}{f'(0.75)} = 0.75 - \frac{0.06640625}{2.6875(43/16)}$ | Attempt Newton-Raphson | M1 |
| | | Correct first application – a correct | |
| | $x_2 = 0.72529(06976) = \frac{499}{688}$ | Correct first application – a correct numerical expression e.g. $0.75 - \frac{\frac{17}{256}}{\frac{43}{16}}$ | A1 |
| | | or awrt 0.725 (may be implied) | |
| | $x_3 = 0.724493 \left(\frac{499}{688} - \frac{0.002015718978}{2.562146811}\right)$ | Awrt 0.724 | A1 |
| | $(\alpha) = 0.724$ | сао | A1 |
| | A final answer of 0.724 with evidence of NR applied twice with no incorrect work should score 5/5 | | (5) |
| | work biourd beare etc | | Total 10 |

| Question Number | Scheme | Notes | Marks |
|--------------------|---|---|---------|
| 3(a) | Focus (4,0) | | B1 |
| | Directrix $x + 4 = 0$ | x + "4" = 0 or x = - "4" | M1 |
| | Directly $x+4=0$ | x + 4 = 0 or x = -4 | A1 |
| | | | (3) |
| (b) | $y = 4x^{\frac{1}{2}} \Rightarrow \frac{dy}{dx} = 2x^{-\frac{1}{2}}$ $y^{2} = 16x \Rightarrow 2y\frac{dy}{dx} = 16$ | $\frac{dy}{dx} = k x^{-\frac{1}{2}}$ $ky \frac{dy}{dx} = c$ | |
| | or $\frac{dy}{dx} = \frac{dy}{dt} \cdot \frac{dt}{dx} = 8 \cdot \frac{1}{8t}$ | their $\frac{dy}{dt} \times \left(\frac{1}{\text{their}\frac{dx}{dt}}\right)$ | M1 |
| | $\frac{dy}{dx} = 2x^{-\frac{1}{2}} \text{ or } 2y \frac{dy}{dx} = 16 \text{ or } \frac{dy}{dx} = 8.\frac{1}{8t}$ | Correct differentiation | A1 |
| | At <i>P</i> , gradient of normal = $-t$ | Correct normal gradient with no errors seen. | A1 |
| | $y - 8t = -t(x - 4t^2)$ | Applies $y - 8t = \text{their } m_N (x - 4t^2)$ or $y = (\text{their } m_N)x + c$ using $x = 4t^2$ and $y = 8t$ in an attempt to find c. Their m_N must be different from their m_T and must be a function of t . | M1 |
| | $y + tx = 8t + 4t^3 *$ | cso **given answer** | A1 |
| | Special case – if the correct gradient is <u>quoted</u> could score M0A0A0M1A1 | | (5) |
| | | | Total 8 |

| Question Number | Scheme | Notes | Marks | |
|--------------------|--|---|----------|--|
| 4(a) | $ \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} 1 & 2 & 2 \\ 1 & 1 & 4 \end{pmatrix} = \begin{pmatrix} 1 & 1 & 4 \\ 1 & 2 & 2 \end{pmatrix} $ | Attempt to multiply the right way round with at least 4 correct elements | M1 | |
| | T' has coordinates (1,1), (1,2) and (4,2) or $\begin{pmatrix} 1\\1 \end{pmatrix}, \begin{pmatrix} 1\\2 \end{pmatrix}, \begin{pmatrix} 4\\2 \end{pmatrix}$ NOT just $\begin{pmatrix} 1 & 1 & 4\\1 & 2 & 2 \end{pmatrix}$ | Correct coordinates or vectors | A1 | |
| (1) | | | (2) | |
| (b) | | Reflection | B1 | |
| | Reflection in the line $y = x$ | y = x | B1 | |
| | Allow 'in the axis' 'about the line' $y = x$ etc. Provided bot reference to the origin unless there is a c | | | |
| | | | (2) | |
| (c) | (4 -2)(1 2)(-2 0) | 2 correct elements | M1 | |
| | $\mathbf{QR} = \begin{pmatrix} 4 & -2 \\ 3 & -1 \end{pmatrix} \begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix} = \begin{pmatrix} -2 & 0 \\ 0 & 2 \end{pmatrix}$ | Correct matrix | A1 | |
| | Note that $\mathbf{RQ} = \begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix} \begin{pmatrix} 4 & -2 \\ 3 & -1 \end{pmatrix} = \begin{pmatrix} 10 \\ 24 \end{pmatrix}$ | $ \begin{array}{c} -4 \\ -10 \end{array} $ scores M0A0 in (c) but | | |
| | allow all the marks in (d) and (e) | 1 | | |
| | | | (2) | |
| (d) | $\det\left(\mathbf{QR}\right) = -2 \times 2 - 0 = -4$ | "-2"x"2" – "0"x"0" | M1 | |
| | | -4 | A1 (2) | |
| | Answer only scores 2/2 | | | |
| | $\frac{1}{\det(\mathbf{QR})}$ scores M | 0 | | |
| (e) | Area of $T = \frac{1}{2} \times 1 \times 3 = \frac{3}{2}$ | Correct area for T | B1 | |
| | 3 | Attempt at " $\frac{3}{2}$ "×±"4" | M1 | |
| | Area of $T'' = \frac{3}{2} \times 4 = 6$ | 6 or follow through their det(QR) x Their triangle area provided area > 0 | A1ft | |
| | | | (3) | |
| | | | Total 11 | |

| Question Number | Scheme | Notes | Marks |
|--------------------|---|---|-----------------|
| 5(a) | $(z_2) = 3 - i$ | | B1 |
| | $(z - (3+i))(z - (3-i)) = z^2 - 6z + 10$ | Attempt to expand $(z - (3 + i))(z - (3 - i))$ or any valid method to establish the quadratic factor e.g. $z = 3 \pm i \Rightarrow z - 3 = \pm i \Rightarrow z^2 - 6z + 9 = -1$ $z = 3 \pm \sqrt{-1} = \frac{6 \pm \sqrt{-4}}{2} \Rightarrow b = -6, c = 10$ Sum of roots 6, product of roots 10 $\therefore z^2 - 6z + 10$ | M1 |
| | $(z^2 - 6z + 10)(z - 2) = 0$ | Attempt at linear factor with their <i>cd</i> in $(z^2 + az + c)(z + d) = \pm 20$ Or $(z^2 - 6z + 10)(z + a) \Rightarrow 10a = -20$ Or attempts f(2) | M1 |
| | $(z_3) = 2$ | | A1 |
| | Showing that $f(2) = 0$ is equivalent to so 4 marks quite easily e.g. $z_2 = 3 - i$ B1, s Answers only can score 4/4 | coring both M's so it is possible to gain all shows $f(2) = 0$ M2, $z_3 = 2$ A1. | (4) |
| 5(b) | -0.5 -1 -1.5 First B1 for plotting (3, 1) and (3, -1) corr with coordinates (allow points/lines/cross on imaginary axis. | 3,1 $3,1$ $3,1$ $3,3$ $3,5$ Re $3,1$ $3,1$ rectly with an indication of scale or labelled ses/vectors etc.) Allow <i>i/-i</i> for 1/-1 marked lative to the conjugate pair with an indication ast 2 | B1 B1 (2) |
| | | | Tota l 6 |

| Question Number | Scheme | | Notes | Marks |
|--------------------|---|--|---|----------|
| 6(a) | $n = 1, LHS = 1^3 = 1, RHS = \frac{1}{4} \times 1^2 \times 2^2 = 1$ | Shows both LHS = 1 and RHS = 1 | | B1 |
| - | Assume true for $n = k$ | | | |
| - | When $n = k + 1$ | | | |
| | $\sum_{r=1}^{k+1} r^3 = \frac{1}{4}k^2(k+1)^2 + (k+1)^3$ | Adds $(k + 1)^3$ to t | he given result | M1 |
| | 1 | Attempt to factor | T | dM1 |
| | $=\frac{1}{4}(k+1)^{2}[k^{2}+4(k+1)]$ | Correct expression | n with | |
| | + | $\frac{1}{4}(k+1)^2$ factoris | ed out. | A1 |
| | $=\frac{1}{4}(k+1)^{2}(k+2)^{2}$ | • • • | coof with no errors and | |
| | Must see 4 things: <u>true for $n = 1$,</u> <u>assumption true for $n = k$, said true for</u> | comment. All the previous marks must have been scored. | | A1cso |
| | $\underline{n = k + 1}$ and therefore true for all \underline{n} | | • | (7) |
| | See extra notes for a | alternative approa | aches | (5) |
| (b) | $\sum (r^3 - 2) = \sum r^3 - \sum 2$ | Attempt two sum | S | M1 |
| | $\sum r^3 - \sum 2n$ is M0 | | | |
| | $=\frac{1}{4}n^{2}(n+1)^{2}-2n$ | Correct expressio | n | A1 |
| | $= \frac{1}{4}n^{2}(n+1)^{2} - 2n$ $= \frac{n}{4}(n^{3} + 2n^{2} + n - 8) *$ | Completion to printed answer with no errors seen. | | A1 |
| - | | | | (3) |
| (c) | $\sum_{r=20}^{r=50} (r^3 - 2) = \frac{50}{4} \times 130042 - \frac{19}{4} \times 7592$ | Attempt $S_{50} - S_{20}$ substitutes into a least once. | or $S_{50} - S_{19}$ and correct expression at | M1 |
| | (=1625525-36062) | Correct numerica (unsimplified) | l expression | A1 |
| | = 1 589 463 | cao | | A1 |
| | | | | (3) |
| (c) Way 2 | $\sum_{r=20}^{r=50} (r^3 - 2) = \sum_{r=20}^{r=50} r^3 - \sum_{r=20}^{r=50} (2) = \frac{50^2}{4} \times 51^2 - \frac{100}{4} \times 51$ | $-\frac{19^2}{4} \times 20^2 - 2 \times 31$ | $\begin{array}{l} M1 \mbox{ for } (S_{50}-S_{20} \mbox{ or } S_{50} \\ -S_{19} \mbox{ for cubes}) - (2x30 \\ \mbox{ or } 2x31) \\ A1 \mbox{ correct numerical} \\ \mbox{ expression} \end{array}$ | Total 11 |
| | =1 589 463 | | A1 | |

| Question Number | Scheme | Notes | Marks |
|--------------------|---|---|---------|
| 7(a) | $u_2 = 3, \ u_3 = 7$ | | B1, B1 |
| | | | (2) |
| (b) | At $n = 1$, $u_1 = 2^1 - 1 = 1$ and so result true for $n = 1$ | | B1 |
| | Assume true for $n = k$; $u_k = 2^k - 1$ | | |
| | and so $u_{k+1} (= 2u_k + 1) = 2(2^k - 1) + 1$ | Substitutes u_k into u_{k+1} (must see this line) | M1 |
| | and so $u_{k+1} (= 2u_k + 1) = 2(2 - 1) + 1$ | Correct expression | A1 |
| | $u_{k+1} \left(= 2^{k+1} - 2 + 1 \right) = 2^{k+1} - 1$ | Correct completion to $u_{k+1} = 2^{k+1} - 1$ | A1 |
| | Must see 4 things: <u>true for $n = 1$,</u> <u>assumption true for $n = k$, said true for</u> <u>$n = k + 1$</u> and therefore <u>true for all n</u> | Fully complete proof with no errors and comment. All the previous marks in (b) must have been scored. | A1cso |
| | Ignore any subsequent attempts e.g. u_{t} | $u_{k+2} = 2u_{k+1} + 1 = 2(2^{k+1} - 1) + 1$ etc. | (5) |
| | | | Total 7 |

| Question Number | Scheme | | Notes | Marks |
|--------------------|--|---|--|----------|
| 8(a) | $\det(\mathbf{A}) = 3 \times 0 - 2 \times 1 (= -2)$ | Correct attempt at the determinant | | M1 |
| | $det(\mathbf{A}) \neq 0$ (so A is non singular) | det(A) = -2 a | nd some reference to zero | A1 |
| | $\frac{1}{\det(\mathbf{A})}$ | scores M0 | | (2) |
| (b) | $\mathbf{B}\mathbf{A}^2 = \mathbf{A} \Rightarrow \mathbf{B}\mathbf{A} = \mathbf{I} \Rightarrow \mathbf{B} = \mathbf{A}^{-1}$ Recognising the | | that \mathbf{A}^{-1} is required | M1 |
| | 1(3-1) | At least 3 cor | rect terms in $\begin{pmatrix} 3 & -1 \\ -2 & 0 \end{pmatrix}$ | M1 |
| | $\mathbf{B} = -\frac{1}{2} \begin{pmatrix} 3 & -1 \\ -2 & 0 \end{pmatrix}$ | $\frac{1}{\text{their det}(A)} \left(\frac{1}{1 + 1} \right)$ | (* *) * *) | B1ft |
| | | Fully correct | | A1 (4) |
| | | er only score 4/- | | Total 6 |
| (b) Way 2 | Ignore poor matrix algebra $\mathbf{A}^{2} = \begin{pmatrix} 2 & 3 \\ 6 & 11 \end{pmatrix}$ | | Correct matrix | B1 |
| | $\begin{pmatrix} 6 & 11 \end{pmatrix} \\ \begin{pmatrix} a & b \\ c & d \end{pmatrix} \begin{pmatrix} 2 & 3 \\ 6 & 11 \end{pmatrix} = \begin{pmatrix} 0 & 1 \\ 2 & 3 \end{pmatrix} \Rightarrow \begin{matrix} 2a+6b=0 \\ 3a+11b=1 \end{matrix} o$ | 2c + 6d = 2 $3c + 11d = 3$ | 2 equations in a and b or 2 equations in c and d | M1 |
| | $a = -\frac{3}{2}, b = \frac{1}{2}, c = 1, d = 0$ | | M1 Solves for a and b or c and d | M1A1 |
| | 2 2 | | A1 All 4 values correct | |
| (b) Way 3 | $\mathbf{A}^2 = \begin{pmatrix} 2 & 3 \\ 6 & 11 \end{pmatrix}$ | | Correct matrix | B1 |
| | $\left(\mathbf{A}^{2}\right)^{-1} = \frac{1}{"2"\times"11"-"3"\times"6"} \begin{pmatrix} "11" & "-1" \\ "-6" & "2" \end{pmatrix}$ | 3")see note | Attempt inverse of \mathbf{A}^2 | M1 |
| | $\mathbf{A}(\mathbf{A}^{2})^{-1} = \frac{1}{4} \begin{pmatrix} 0 & 1 \\ 2 & 3 \end{pmatrix} \begin{pmatrix} 11 & -3 \\ -6 & 2 \end{pmatrix} or \frac{1}{4} \begin{pmatrix} 11 \\ -6 \end{pmatrix}$ | $ \begin{array}{c} -3\\2 \end{array} \begin{pmatrix} 0 & 1\\2 & 3 \end{pmatrix} $ | Attempts $\mathbf{A}(\mathbf{A}^2)^{-1} or(\mathbf{A}^2)^{-1} \mathbf{A}$ | M1 |
| | $\mathbf{B} = -\frac{1}{2} \begin{pmatrix} 3 & -1 \\ -2 & 0 \end{pmatrix}$ | | Fully correct answer | A1 |
| (b) War 4 | | | Descentistics (by DA T | D1 |
| (b) Way 4 | | 2d = 0 $c + 3d = 1$ | Recognising that $BA = I$ 2 equations in a and b or 2 equations in c and d | B1 M1 |
| | $ \begin{pmatrix} a & b \\ c & d \end{pmatrix} \begin{pmatrix} 0 & 1 \\ 2 & 3 \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \Rightarrow \begin{cases} 2b = 1 \\ a + 3b = 0 \end{cases} $ $ a = -\frac{3}{2}, b = \frac{1}{2}, c = 1, d = 0 $ | | M1 Solves for a and b or c and d | M1A1 |
| | | | A1 All 4 values correct | |

| Question Number | Scheme | Notes | Marks | |
|--------------------|---|---|---------|--|
| 9 (a) | $y = 9x^{-1} \Longrightarrow \frac{\mathrm{d}y}{\mathrm{d}x} = -9x^{-2}$ | $\frac{\mathrm{d}y}{\mathrm{d}x} = k \; x^{-2}$ | | |
| | $xy = 9 \Longrightarrow x\frac{\mathrm{d}y}{\mathrm{d}x} + y = 0$ | Correct use of product rule. The sum of two terms, one of which is correct. | M1 | |
| | or $\frac{dy}{dx} = \frac{dy}{dt} \cdot \frac{dt}{dx} = \frac{-3}{p^2} \cdot \frac{1}{3}$ | their $\frac{dy}{dt} \times \left(\frac{1}{\text{their}\frac{dx}{dt}}\right)$ | | |
| | $\frac{dy}{dx} = -9x^{-2} \text{ or } x \frac{dy}{dx} + y = 0 \text{ or } \frac{dy}{dx} = \frac{-3}{p^2} \cdot \frac{1}{3}$ | Correct differentiation. | A1 | |
| | | Applies $y - \frac{3}{p} = (\text{their } m)(x - 3p)$ or | | |
| | $y - \frac{3}{p} = -\frac{1}{p^2}(x - 3p)$ | y = (their m)x + c using x=3p and y = $\frac{3}{n}$ in an attempt to find c. | M1 | |
| | | Their <i>m</i> must be a function of <i>p</i> and come from their dy/dx. | | |
| | $x + p^2 y = 6p *$ | Cso **given answer** | A1 | |
| | Special case – if the correct gradient is <u>quoted</u> could score M0A0M1A1 | | | |
| (b) | $x + q^2 y = 6q$ | Allow this to score here or in (c) | B1 | |
| | | | (1) | |
| (c) | $6p - p^2 y = 6q - q^2 y$ | Attempt to obtain an equation in one variable <i>x</i> or <i>y</i> | M1 | |
| | $y(q^{2} - p^{2}) = 6(q - p) \Rightarrow y = \frac{6(q - p)}{q^{2} - p^{2}}$ $x(q^{2} - p^{2}) = 6pq(q - p) \Rightarrow x = \frac{6pq(q - p)}{q^{2} - p^{2}}$ | | M1 | |
| | $y = \frac{6}{p+q}$ | One correct simplified coordinate | A1 | |
| | $x = \frac{6pq}{p+q}$ | Both coordinates correct and simplified | A1 | |
| | | | (4) | |
| | | | Total 9 | |

Extra Notes

6(a) To show equivalence between $\frac{1}{4}k^2(k+1)^2 + (k+1)^3$ and $\frac{1}{4}(k+1)^2(k+2)^2$

$$\frac{1}{4}k^{2}(k+1)^{2} + (k+1)^{3} = \frac{1}{4}k^{4} + \frac{3}{2}k^{3} + \frac{13}{4}k^{2} + 3k + 1$$

Attempt to expand one correct expression up to a quartic M1

$$\frac{1}{4}(k+1)^2(k+2)^2 = \frac{1}{4}k^4 + \frac{3}{2}k^3 + \frac{13}{4}k^2 + 3k + 1$$

| Attempt to expand both correct expressions up to a quartic | M1 |
|--|----|
| One expansion completely correct (dependent on both M's) | A1 |
| Both expansions correct and conclusion | A1 |

Or

To show
$$\frac{1}{4}(k+1)^2(k+2)^2 - \frac{1}{4}k^2(k+1)^2 = (k+1)^3$$

 $\frac{1}{4}(k+1)^2(k+2)^2 - \frac{1}{4}k^2(k+1)^2$ Attempt to subtract M1
 $\frac{1}{4}(k+1)^2(k+2)^2 - \frac{1}{4}k^2(k+1)^2 = k^3 + 3k^2 + 3k + 1$ Obtains a cubic expression M1
 $\frac{1}{4}(k+1)^2(k+2)^2 - \frac{1}{4}k^2(k+1)^2 = (k+1)^3$ Correct completion and comment A1

8(b) Way 3

Attempting inverse of \mathbf{A}^2 needs to be recognisable as an attempt at an inverse

E.g
$$(\mathbf{A}^2)^{-1} = \frac{1}{Their \, Det(\mathbf{A}^2)} (A \, changed \, \mathbf{A}^2)$$

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