## GCE Examinations

## Advanced Subsidiary / Advanced Level

## Mechanics <br> Module M1

## Paper G

## MARKING GUIDE

This guide is intended to be as helpful as possible to teachers by providing concise solutions and indicating how marks should be awarded. There are obviously alternative methods that would also gain full marks.

Method marks (M) are awarded for knowing and using a method.
Accuracy marks (A) can only be awarded when a correct method has been used.
(B) marks are independent of method marks.

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## M1 Paper G - Marking Guide

1. 


resolve $\uparrow: R+T=10 g ; R+\frac{3}{2} R=10 g$
M2
$\frac{5}{2} R=10 g ; \therefore R=4 g$ so $T=6 g$ A1
moments about pivot: $10 g x-4(6 g)=0$
$10 g x=24 g$, so $x=2.4$ and hence c.o.m. is 4.4 m from $A$
2. (a) mass of ball remains constant, force is constant
$\boldsymbol{F}=m \boldsymbol{a}$ so $\boldsymbol{a}$ constant
(b)
(i) $\quad \boldsymbol{a}=\frac{\Delta \boldsymbol{v}}{t}=\frac{1}{4}[(10 \mathbf{i}+9 \mathbf{j})-(2 \mathbf{i}-3 \mathbf{j})]=2 \mathbf{i}+3 \mathbf{j}$
M1 A1
mag. of $\boldsymbol{a}=\sqrt{ }\left(2^{2}+3^{2}\right)=\sqrt{ } 13=3.61 \mathrm{~ms}^{-2}(3 \mathrm{sf})$
M1 A1
(ii) $\boldsymbol{F}=m \boldsymbol{a}=2(2 \mathbf{i}+3 \mathbf{j})=4 \mathbf{i}+6 \mathbf{j}$
req'd angle $=\tan ^{-1} \frac{3}{2}=56.3^{\circ}(3 \mathrm{sf})$
M1

M1 A1 (9)
3. (a) particle

B1
(b)

resolve // to plane: $P \cos 10^{\circ}-3 g \sin \alpha=0$
M1 A1
$P \cos 10^{\circ}=3 g\left(\frac{3}{5}\right) \therefore \mathrm{P}=17.9(1 \mathrm{dp})$
M1 A1
(c) resolve perp. to plane: $R+P \sin 10^{\circ}-3 g \cos \alpha=0$

M1 A1
$R=3 g\left(\frac{4}{5}\right)-P \sin 10^{\circ}=20.4 \mathrm{~N}(1 \mathrm{dp})$
M1 A1
4. (a) cons. of mom. $0.05(400)=(0.05+4.95) v$
(b) $R=m g ;{ }^{-} F=m a \quad$ M1
but $F=\mu R ; \therefore a=\frac{-\mu R}{m}=\frac{-\mu m g}{m}={ }^{-} \mu g \quad$ M1 A1
use with $u=4, v=0, s=4$ M1
$v^{2}=u^{2}+2 a s$, so $0=16-8 \mu g$
M1
$\mu=\frac{16}{8 g}=\frac{2}{g}$
5. (a) disp. of F rel to $\mathrm{G}=[(2 t-3)-2] \mathbf{i}+(t-5) \mathbf{j}=(2 t-5) \mathbf{i}+(t-5) \mathbf{j}$

M1 A1
(b) $d^{2}=(2 t-5)^{2}+(t-5)^{2}$

M1
$=4 t^{2}-20 t+25+t^{2}-10 t+25=5 t^{2}-30 t+50$
M1 A1
$=5\left(t^{2}-6 t+10\right)=5\left[(t-3)^{2}+1\right]$
M2
$\min . d^{2}($ and hence $d)$ when $t=3$
(c) when $t=3, d^{2}=5$

M1 A1
dist. $=\sqrt{ } 5=2.24 \mathrm{~m}(3 \mathrm{sf})$
A1
(11)
6. (a) speed


B2
(b) using $v=u+$ at with $v=2 U, u=5 U, t=6$ gives $1^{\text {st }}$ decel. $=\frac{1}{2} U \mathrm{~ms}^{-2}$

M1 A1
using $v=u+a t$ with $v=0, u=2 U, t=2$ gives $2^{\text {nd }}$ decel. $=U \mathrm{~ms}^{-2}$
M1 A1
(c) area under graph $=$ dist. travelled $=220 \mathrm{~m}$
$\frac{1}{2}(6)(3 U)+22(2 U)+\frac{1}{2}(2)(2 U)=220$
M1 A2
$55 U=220 \quad \therefore U=4 \mathrm{~ms}^{-1}$
M1 A1
7.

(a) $M_{C}: M_{T}=1200: 800=3: 2 \quad R_{C}=300 \mathrm{~N} \therefore R_{T}=200 \mathrm{~N}$

M1 A1
(b) for car and trailer, eqn. of motion is $3000-500=2000 a$

M1
giving $a=\frac{5}{4} \mathrm{~ms}^{-2}$
M1 A1
(c) for car, eqn. of motion is $3000-300-T=1200 \times \frac{5}{4}$

M1
giving $T=1200 \mathrm{~N}$
M1 A1
(d) total of braking + resistive forces $=1500 \mathrm{~N}$
$-1500=2000 a$ so $a=-\frac{3}{4} \mathrm{~ms}^{-2}$
M1 A1
$u=24, v=0, a=-\frac{3}{4} \quad$ use $v^{2}=u^{2}+2 a s$
M1
$0=576-\frac{3}{2} s \quad \therefore s=384 \mathrm{~m}$
M1 A1
(e) for car $(\leftarrow): T+1000+300=1200\left(\frac{3}{4}\right)$

M1 A1
$T={ }^{-} 400 \mathrm{~N} \therefore T=400 \mathrm{~N}$, pushing the car
M1 A1
(f) e.g. unlikely to be realistic, likely to decrease as speed decreases

B2

## Performance Record - M1 Paper G

| Question no. | 1 | 2 | 3 | 4 | 5 | 6 | 7 | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Topic(s) | moments | $\begin{aligned} & \mathbf{i}, \mathbf{j}, \\ & F=m a \end{aligned}$ | statics | cons. of mom., friction | $\begin{aligned} & \hline \text { rel. } \\ & \text { posn. } \\ & \mathbf{i}, \mathbf{j} \end{aligned}$ | speed time graph, uniform accel. | connected bodies |  |
| Marks | 6 | 9 | 9 | 9 | 11 | 12 | 19 | 75 |
| Student |  |  |  |  |  |  |  |  |
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