GCE Examinations Advanced Subsidiary / Advanced Level

Statistics Module S1

Paper K

MARKING GUIDE

This guide is intended to be as helpful as possible to teachers by providing concise solutions and indicating how marks should be awarded. There are obviously alternative methods that would also gain full marks.

Method marks (M) are awarded for knowing and using a method.

Accuracy marks (A) can only be awarded when a correct method has been used.

(B) marks are independent of method marks.



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S1 Paper K - Marking Guide

1. (a)
$$\frac{11}{16} \times \frac{10}{15} \times \frac{9}{14} = \frac{33}{112}$$
 or 0.295 (3sf) M2 A1

(b)
$$\frac{5}{16} \times \frac{11}{15} \times \frac{4}{14} = \frac{11}{168}$$
 or 0.0655 (3sf) M2 A1

(c)
$$3 \times \frac{5}{16} \times \frac{11}{15} \times \frac{10}{14} = \frac{55}{112}$$
 or 0.491 (3sf) M3 A1 (10)

2. (a)
$$S_{AA} = 10131 - \frac{703^2}{50} = 246.82$$
 M1

$$S_{HH} = 1338.5 - \frac{217^2}{50} = 396.72$$
 M1

$$S_{AH} = 3253.5 - \frac{703 \times 217}{50} = 202.48$$
 M1

$$r = \frac{202.48}{\sqrt{246.82 \times 396.72}} = 0.6471$$
 M1 A1

r is strongly +ve showing that older pupils tend to do more homework B1

- (b) e.g. younger pupils are set less homework and also do little or no paid work etc. apparent correlation is because both correlate with age B2
- (c) e.g. collect data from one year group, likely to have similar amounts of homework set, so will see effect of paid work B2 (10)

3. (a) midpoints: 20, 60, 100, 140, 180, 250, 350, 500 M1
$$\sum fm = 8060$$
 A1

$$mean = \frac{8060}{92} = 87.6 \text{ (3sf)}$$
 M1 A1

$$\sum fm^2 = 1700600$$
 A1

std. dev. =
$$\sqrt{\frac{1700600}{92} - (87.609)^2} = 104 \text{ (3sf)}$$
 M2 A1

- (b) e.g. data very skewed, mean and std. dev. strongly affected by a few very large values B2
- (c) e.g. median and IQR B1 (11)

4. (a)
$$P(Z < \frac{20-21.6}{1.8}) = P(Z < 0.89) = 0.1867$$
 M2 A1

(b)
$$P(Z > \frac{24-21.6}{1.8}) = P(Z > 1.33) = 0.0918$$
 M1 A1

$$\therefore \text{ in 90 days expect } 0.0918 \times 90 = 8.26 \therefore 8 \text{ times}$$
 M1 A1

(c)
$$P(X < 24 \mid X > 22) = \frac{P(22 < X < 24)}{P(X > 22)}$$
 M1 A1

$$P(X > 22) = P(Z > \frac{22 - 21.6}{1.8}) = P(Z > 0.22) = 0.4129$$
 M1 A1

$$P(22 < X < 24) = P(X > 22) - P(X > 24) = 0.3211$$
 M1

: require
$$\frac{0.3211}{0.4129} = 0.778$$
 (3sf) A1 (13)

5. 8, 4, 3, 1 (a)

A1

(b) 4 months A1

n = 31; $Q_1 = 8^{th} = 6$ months (c) $Q_2 = 16^{th} = 15 \text{ months}$ $Q_3 = 24^{th} = 30 \text{ months}$ M1 A1 A1 **A**1

- M1
- (d) $Q_3 - Q_1 = 30 - 6 = 24$ limits are $6 - (1.5 \times 24) = 30$ and $30 + (1.5 \times 24) = 66$ ∴ 70 is an outlier
- M1 **A**1

- (e) 0 10 20 70
- В3

(f)+ve skew

- B1
- e.g. lot of people unemployed for a short time, only a few for a long time B1
- (14)

6. (a) discrete uniform B1

(b) 2 **A**1

 $\sum bP(b) = \frac{1}{2} + \frac{1}{2} + \frac{3}{4} = \frac{7}{4}$ (c)

M1 A1

 $P(C=2) = P(A=1 \text{ and } B=1) = \frac{1}{3} \times \frac{1}{2} = \frac{1}{6}$ (d)

M2 A1

- $P(C=3) = (\frac{1}{3} \times \frac{1}{4}) + (\frac{1}{3} \times \frac{1}{2}) = \frac{1}{4}$ (e)
 - $P(C=4) = (\frac{1}{3} \times \frac{1}{4}) + (\frac{1}{3} \times \frac{1}{4}) + (\frac{1}{3} \times \frac{1}{2}) = \frac{1}{3}$
 - $P(C=5) = (\frac{1}{3} \times \frac{1}{4}) + (\frac{1}{3} \times \frac{1}{4}) = \frac{1}{6}$
 - $P(C=6) = (\frac{1}{3} \times \frac{1}{4}) = \frac{1}{12}$

- M3 A3
- $E(C) = \sum cP(c) = \frac{1}{3} + \frac{3}{4} + \frac{4}{3} + \frac{5}{6} + \frac{1}{2} = \frac{15}{4}$ (f)

M1 A1

 $E(A) + E(B) = 2 + \frac{7}{4} = \frac{15}{4}$:: E(C) = E(A) + E(B)

M1 A1 **(17)**

Total (75)

Performance Record – S1 Paper K

Question no.	1	2	3	4	5	6	Total
Topic(s)	probability	pmcc	mean and std. dev.	normal dist.	stem & leaf, quartiles, boxplot	discrete r. v.	
Marks	10	10	11	13	14	17	75
Student							